## Water Simulation and Rendering in the VR Film, 'Arden's Wake'

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This talk is about water simulation and rendering in Arden's Wake


The entire set of Arden's Wake is on or below an infinite world of water.
Things interact with the water surface (boats, splashes, etc).
Underwater scenes have key volumetric lighting elements.
There is a lot of complexity in the non water assets, such as characters, sets, FX, and set lighting, so all solutions need to be high performance.


Here is a screenshot from a bottleneck scene where there is a lot going on.


Here are all the elements this talk will cover, highlighted with yellow arrows.
Foam - dynamic whitewater simulation coming off the boat wake
Boat wake - dynamic fluid simulation using a solution to the shallow water equations
Ocean waves - Ambient ocean waves
Splashes - Baked out and dynamic splash simulations
Underwater rendering - Volumetric passes for the murky underwater look
Volumetric spotlights - Seem in green in the upper right hand corner, used in a variety of contexts

We will cover both the underwater rendering and water simulation done for Arden's Wake.


We'll first talk about the underwater rendering.


This is some artwork from Arden's Wake. We wanted a fully volumetric underwater look with realistic sunlight filtering through the water, fully volumetric spotlights, and compositing with FX and translucent geometry.


Here is an actual render from Arden's Wake that demonstrates the properties mentioned in the previous slide. aGOC 2018

## Directional Lights

Inspiration
[Hoobler 16] - Volumetric rendering at Nvidia
[Hillaire 15] - Volumetric rendering in Frostbite
Sunlight illuminating water
Colored transmittance
Analytical solution

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We needed to have environment lighting from the sun with light that transmits through the water.
Inspiration - Nathan Hoobler and Sebastian Hillaire gave great explanations of volume rendering, and their slides are available online.

We used a directional light formulation, built off of existing work, but extended it with a closed form solution in a constrained setup.
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## Directional Lights



On the top, the yellow arrow represents the direction of the light, which is constrained to be in the -z direction. The blue line is the water surface height in $z$.

The ray we are computing the lighting for starts at the green circle and follows the red arrow.
The gray object is underwater, and terminates the ray.

## Numerical Solution



In many rendering solutions, we'd ray march this, computing the integrand of the integral defining the lighting equation for this setup at each purple dot along the red ray. For underwater environments, this can be prohibitively slow for a real time solution.

## Analytical Solution

$$
\begin{gathered}
\int_{0}^{d} L \mathrm{e}^{-\mu \alpha\left(w_{z}-\left(p_{z}+v_{z} t\right)\right)} \mathrm{e}^{-\mu t} d t \\
= \\
\frac{L \mathrm{e}^{\mu \alpha\left(p_{z}-w_{z}\right)}}{\mu\left(\alpha v_{z}-1\right)}\left(\mathrm{e}^{\mu\left(\alpha v_{z}-1\right) d}-1\right)
\end{gathered}
$$

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If we solve the above integral, we get a closed form solution for the directional light described.

Here are the parameters for the integral:
d - maximum distance along the ray until the ray terminates.
L - Radiance of the directional light
mu - density of the medium
alpha - density multiplier for the attenuation of the light as it travels from the water surface down through the water
w_z - water height in z
$\mathrm{p} \_\mathrm{z}-\mathrm{z}$ coordinate of the ray start
$\mathrm{v} \_\mathrm{z}-\mathrm{z}$ component of the direction of the ray
t - distance along the ray
The analytical solution can be coded simply in a shader with about 30 instructions rather than 2000+ for a slow ray marching solution with 100 samples that still gives artifacts.


This is an example of how the color shifts as you get deeper underwater. This video (and others described in these slides) can be seen in the recording of the talk.

## Spotlights <br> Attempts at sampling <br> Brute force marching <br> Trapezoidal rule <br> Different quadrature Equiangular sampling <br> [Kulla 11]



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The need to view the spotlights from all angles means we must have good integration schemes.
No proxy geometry or cards will be usable due to artifacts in VR, so must use a fully volumetric solution.
There is no closed form analytical solution like previous slides, but one can use look up tables for some formulations of spotlights.

Brute force ray marching lead to artifacts.

We settled for equiangular sampling, which is a way of importance sampling lights in homogenous mediums. The technique places samples in an intelligent way such that they have a maximal impact on the final integration result. It is also very easy to code and very efficient.

## Trapezoidal Rule



This is rendering a spotlight from the perspective of the red arrow on the right using trapezoidal rule quadrature for ray marching.

Note the noticeable edge in the beam with the yellow arrow pointing to it.
This is an artifact due to undersampling, but we can't afford more samples.

## Trapezoidal Rule + Equiangular



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This example uses the same number of samples in the previous slide, but with equiangular sampling.
Note how the beam now looks smooth and there is no artifact.
There is no noticeable performance degradation due to the simplistic implementation.
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## Results

## 16 samples per ray per spotlight

~.1-. 2 ms per eye per spotlight
.33 ms per eye
directional light
1 spotlight
compositing dithering [Gjoel 16] ambient light


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Overall, the volume rendering pass takes .33 ms per eye.
Dithering is important due to how dark our sets are, and the talk slides cited about the rendering for the game Inside gives great insight into this topic.


Next we will discuss the water simulation techniques used on Arden's Wake.
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## Ocean Waves

Procedural method [Tessendorf 01]
No repeated waves in time
Tiles nicely


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Tessendorf's technique for ocean waves is great for this type of setup with a large ocean plane.
It doesn't need to be simulated, and you don't notice tiling and looping if setup correctly.
There are plenty of example implementations that can be found online.

## Water Simulation

3d simulation (too slow)
bake out simulations (too much memory)
Various tricks (don't look good)
[Bridson 16] - Shallow water equations


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For simulated elements, we needed to choose a solution that was lightweight but gave us nice properties like surface velocities.

We choose to implement a shallow water simulator, which is a 2d fluid simulation technique.
The simulation domain is defined as a 2d grid of cells.
Cells are either occupied by water or colliders, and 2 d velocities flow on the surface of the water.

Robert Bridson's book on fluid simulation for computer graphics has great descriptions of algorithms.

## Initial State



We will walk through a simplified simulation step in a slice through the simulation domain with a ball dropping in some undisturbed water.

The orange ball is falling straight down into the fluid with a downward velocity in green.

## Calculate Overlap Volume



Once the ball is intersecting the fluid, we must determine the overlap volume outlined in red.
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## Redistribute Overlap Volume



P=NROSE

We take the overlap volume and distribute to neighboring cells.
Note that for performance reasons, we limit the distance we distribute.
Also, note cells that overlap the collider get a height value because we extrapolate height into colliders for velocity stability. Please see referenced literature for more information on this.

## Update Velocity



We update velocity based on a finite difference of the height.
We get velocities propegating outward as expected.

## Update Height



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studios

We update water height according to finite differences of the velocity. You can see the formation of waves.
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## Output



## PENROS: <br> stuoios

You can push fluid down under the collider only at output time, but you don't propagate this back to the next solver step.
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## Overlap Volume Problem



Here are 4 examples of a sphere overlapping the water plane at different depths.
Note that from 1 to 4 the overlap volume increases.

## Incorrect Collision Mask



1


2


3


4

## PENROS: <br> stuoios

There are a few problems with calculating overlap volume in the fashion previously described.
Yellow show the cells the solver considers as being in a collision state. Note that qualitatively these don't represent what you see intersecting the water surface, especially in \#4 where the ball is completely underwater.

## Too Much Displaced Volume



1


2


3


4

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There are also issues with what happens when we redistribute the overlap volume.
Note that as the sphere gets buried deeper in the water, more fluid is displaced, which is intuitively wrong.

Imagine swimming near the surface of the water, kicking hard. You get a lot of disturbance of the water
Now imagine diving deep under the water and kicking just as hard. You don't see nearly as much disturbance, but with this model, you'd see more.
The goal is to come up with a collision model that qualitatively does what we'd expect while maintaining the simple simulator framework.


This video shows using the incorrect collision model for this sub falling in the water with the red proxy sphere used for collisions. Note that in this case, as the sub descended fully underwater, you notice cells at the surface propagating waves that are too large, and artifacts for the cells that are considered to be in a collision state.
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## Overlap Volume Fix



1


2


3


4

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To fix this problem, when the sphere is more than half underwater, we take the overlap volume equal to the portion above water.

Look at 3 where the overlap volume is mirror of what is above surface.

## Correct Collision Mask



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The collision mask represents what is seen above water (look at 3).
4 has no collision since it is fully submerged.
This gives roughly what we'd expect visually.
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## Correct Displacement



1


2


3


4
$P=N R O S E$

Also, this method attenuates the distribution of overlap volume to zero when the sphere is completely underwater.

Volume displacement attenuates to zero as it gets deeper, until there is no displacement in \#4. Note that the overlap volume peaks at 2


This video demonstrates the same sub falling into the water, but with the improved collision model. There are smaller surface waves as the sub fully submerges, and you don't notice residual collision artifacts once the sub is fully submerged.

## Comparison



This compares the two videos side by side.

## Real-time Considerations

## Must use 32 bit buffers

## Constraints on domain size



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There are important things to consider when creating a simulator such as this in a real-time environment.

Anything less than 32 bits per channel for height and velocity will cause instability, and the resulting simulation will explode.

In the image on the left, the boat is causing a wake, with water displacement height in red, across a large area. The image on the right shows where the viewer is watching a fish splash in the water.

While this could be solved with multiple domains, unfortunately, we could only afford one due to performance considerations. Also, we could only afford $512 \times 512$ for our domain size. Thus, it is hard to get enough resolution to correctly resolve all simulated elements.


This was a video of the fish falling in the water from the previous slide. Note that the splash looked low resolution.


We bake out a Houdini FLIP simulation and composite it in with the water surface. The result looks much better.

## Comparison



This is a side by side comparison video of the two splashes.
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## Static Depth Map Colliders

Bake out static collision mask
Parent to moving geometry
Sample to collision grid
Great for boat wakes


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For a boat wake we want to precompute a collision mask for the boat.

First, we determine how much the boat falls below the base waterline.
Next, we bake out this data into a 2d image.
Finally, we parent a plane with this image to the moving boat, and resample the collision depth to the simulation domain.


This is a video of a boat wake and foam simulation.


Moving colliders can be baked out into a texture atlas.
This is an example of a character swimming in water, and we compute the penetration depth per frame of her in relation to the water plane.

This is much better than baking out the sim since we only care about the small patch of water where the character interacts.

Similar to the case with the sphere, we only care when the arms are near the water surface, not necessarily intersecting it directly.


This video shows the simulation of the character swimming in the water.

## Whitewater

Emit based on fluid acceleration [Ihmsen 12] Advect by velocity Dissipation


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We used a simple whitewater model inspired by Ihmsen's paper on a unified solver for spray, foam and air bubbles, which describes techniques used extensively in visual effects.

The basic idea is that we track a scalar field for whitewater, and emit into it according to fluid acceleration. We then advect the whitewater by the fluid velocity, and apply dissipation.

## Results

$512 \times 512$ for height and velocity $1024 \times 1024$ for foam
0.6 ms per frame
0.1 ms for colliders
0.3 ms for integration
0.2 ms for foam

We used a $512 \times 512$ resolution simulation grid for the shallow water elements.
We used a higher resolution foam simulation field since it is cheaper to compute than the water simulation, and it gives nice detail to the overall look.
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## Frame Time



Overall, we use about a quarter of our total frame budget in the worst case for the elements discussed in this talk. Note that we'd also have overhead due to rendering the water surface, and other elements have variable performance, so these numbers are approximate.


This video demonstrates how a user could interact with the fluid if given a VR hand controller. Since the water simulation runs in real time, it is very responsible to user input, and gives a terrific sense of immersion in the world.
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## Citations

[Kulla 11] Importance Sampling of Area Lights in Participating Media, SIGGRAPH 2011
[Hoobler 16] Fast, Flexible, Physically-Based. Volumetric Light Scattering, NVIDIA Developer Technology 2016.
[Hillaire 16] Physically-based \& Unified Volumetric Rendering in Frostbite, SIGGRAPH 2015.
[Tessendorf 01] Simulating Ocean Water, SIGGRAPH 2001.
[Gjoel 16] Low Complexity, High Fidelity - INSIDE Rendering, GDC 2016.
[Bridson 16] Fluid Simulation for Computer Graphics, 2016.
[Ihmsen 12] Unified spray, foam and air bubbles for particle-based fluids, The Visual Computer, 2012.

These are the citations used in this paper.
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## Thanks!

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Thanks everyone!

