# EMBRACING THE DARK ART OF MATHEMATICAL MODELING IN GAME AI

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#### **Administrivia**

- Mid-to-Advanced Level Lecture
- References:
  - 2010 Al Summit Talk: <u>Improving Al Decision Modeling Through Utility Theory</u>
  - I/ITSEC 2011: A Game AI Approach to Autonomous Control of Virtual Characters
    - Best Paper: <u>paper</u> <u>presentation</u>
  - SISO SIW 2012: Introducing GAIA: A Reusable, Extensible Architecture for AI Behavior
    - Not published yet (end of March) search for 12S-SIW-046
  - Behavioral Mathematics for Game AI







## What Is Utility-Based AI?

- Calculate *relative goodness* of each option
  - Shades of gray
  - Finer granularity
  - Subtle nuance of the situation
- Guns and Grenades

– Reasonable Variation => Believability









## **Al Engineering**

- "Like a giant bucket of floats..."
- Utility is complex to the novice
- So is C++!!
- Software Engineering => tools
- We need Utility Engineering



http://www.enasco.com/product/TB15671T

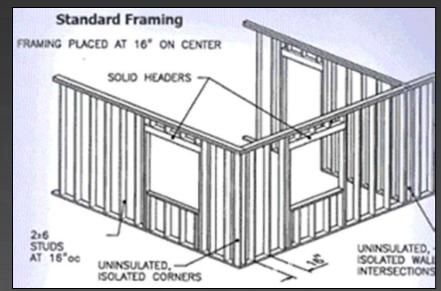






## **Design Patterns**

"Simple and succinct solutions to commonly occurring design problems"
 – Gamma et. al.



http://www.renovation-headquarters.com/walls-partitions.htm







#### **Absolute vs. Relative**

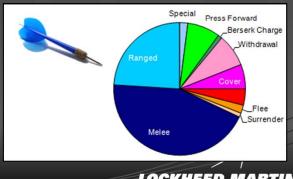
- Absolute Utility ("Rank")
  - Always pick an option with higher rank over one with lower rank
- Relative Utility ("Weight")
  - Every option could be picked, but one with higher utility is more likely
  - "Weighted Random"
- You Can Use Both!!





**Divide Into Categories** 

Calculate "Appropriateness"



## **Dual Utility AI**

1. Eliminate weight <= 0

Completely Inappropriate

2. Screen on rank ←

Something more important is going on

3. Eliminate very small weight

Avoid

4. Weighted Random

**Artificial Stupidity!!** 

Random but Reasonable









#### **Considerations**

- Modular decision making
  - Each consideration examines
    a single aspect of the situation
- Each consideration can:
  - Set a minimum rank
  - Apply a bonus to the weight
  - Apply a multiplier to the weight

$$R_O = Max_{i=1}^n(R_i)$$

$$oxed{W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)}$$







# **Example: Sniper**

- Shoot / No-Shoot
- Shoot Considerations:
  - Clear line of sight
  - Clear line of retreat



http://www.imfdb.org/wiki/Bangkok\_Dangerous









#### Pattern: Opt Out

- Consideration: "Do not do this!!"
- Simply set M = 0

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$







# **Example: Guard**

- Engage Decision
  - He attacks me
  - He attempts to enter
  - Poor chat choice



http://www.histquest.com/index.php?id=51









#### Pattern: Opt In

- Consideration: "Do this!!"
- Stand guard "Default Option"
  - Fixed values: Rank 0, Weight 1
- Engage
  - Default R = -1
  - Each consideration can set R = 10

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$









#### **Pattern: Inertia**

- While executing, retain some rank
- Engage
  - Default R = -1
  - Each consideration can set R = 10
  - Execution History consideration
    - Set R = 7 while executing

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_i)$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$







# **Example: Guard**

- Options:
  - Guard
  - Engage
  - Ring the Alarm



http://www.histquest.com/index.php?id=51









#### **Pattern: Commit**

- Like inertia, but increase rank
- Engage / Ring the Alarm
  - Default R = -1
  - Each consideration can set R = 10
  - Execution History consideration
    - Set R = 11 while executing

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$









#### Pattern: Is Done

- "I'm done executing –
   do something else now"
- *Is Done* consideration:
  - Am I currently selected?
  - Have I finished execution?
  - If so, M = 0

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_i)$$

$$W_{O} = \left(\sum_{i=1}^{n} B_{i}\right) \cdot \left(\prod_{i=1}^{n} M_{i}\right)$$







# **Example: Sniper**

- Shoot / No-Shoot
- Shoot Considerations:
  - Clear line of sight
  - Clear line of retreat
  - Delay between shots



http://www.imfdb.org/wiki/Bangkok\_Dangerous









#### Pattern: Cooldown

- Don't do the same thing twice in a row
- Evaluate time since last selection
  - Fixed delay (M = 0 for 15 sec)
  - Variable delay (M = 0 for 10-20 sec)
  - Tiered delay
    - M = 0 for 8-12 sec
    - M = 0.5 for 18-22 sec

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$







# **Example: Sniper**

- Shoot/Wait/Flee
- Shoot Considerations:
  - Clear line of sight
  - Clear line of retreat
  - Delay between shots
  - Number of shots fired











## **Pattern: Repeat Penalty**

- Fire Option Repeat Penalty
  - $R = 10 (2)^* \text{ shots_fired}$
- Flee Option
  - R depends on situation
    - Shooting at me?
    - Looking at me?
- Surrounding me?
- Running away?

- 1) Weight <= 0
- 2) Screen rank
- 3) Very small weight
- 4) Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$









#### **Something Harder**

- **Sniper Target Selection:** 
  - Side < US Military: M = 10 Civilian: M = 0.1

- Rank  $\leftarrow$  Officer: M = 16 - Roo: M = 4 Enlisted: M = 1

- Distance  $\leq \frac{50-300 \text{ meters: } 0.5 \leq M \leq 2}{\text{Otherwise: } M = 0}$ 

— Visibility — M = LOS\_hits / LOS\_attempts



- Screen rank
- 3) Very small weight
- Weighted Random

$$R_O = Max_{i=1}^n(R_{i})$$

$$W_O = \left(\sum_{i=1}^n B_i\right) \cdot \left(\prod_{i=1}^n M_i\right)$$







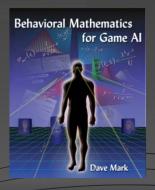
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